| Concrete | Pictorial | Abstract |
| :---: | :---: | :---: |
| Combining two parts to make a whole (use other resources too, e.g. shells, teddy bears, cars) | Children to represent the cubes using dots or crosses. They could put each part on a part whole model too. | $4+3=7$ <br> Four is a part, 3 is a part and the whole is seven. |
| Starting at the bigger number and counting on - using cubes <br> Or numicon.... | A bar model which encourages the children to count on, rather than count all. | The abstract number line: <br> What is 2 more than 4 ? <br> What is the sum of 2 and 4 ? <br> What is the total of 4 and 2? $4+2$ |


| Regrouping to make 10; using ten frames and counters/cubes or using Numicon.$6+5$ |  | Children to draw counter | he ten frame and /cubes. | Children to develop an understanding of equality e.g.$\begin{aligned} & 6+\square=11 \\ & 6+5=5+\square \\ & 6+5=\square+4 \end{aligned}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TO + O using base 10. Continue to develop understanding of partitioning and place value.$41+8$ |  | Children to represent the base 10 e.g. lines for tens and dot/crosses for ones. |  |  | $\begin{aligned} & \hline 41+8 \\ & 1+8=9 \\ & 0+9=49 \\ & +\begin{array}{r} 4 \\ \hline 48 \\ \hline 49 \\ \hline 40 \\ \hline \end{array} \end{aligned}$ |  |
| Conceptual Variation - Different ways to ask children to solve calculations e.g. $21+34$ |  |  |  |  |  |  |
|  $$ | In year and in How m 21 | ord problems: there are 21 children ear 4, there are 34 children. y children in total? $34=55 . \text { Prove it }$ | $\begin{aligned} & \begin{array}{l} 21 \\ +34 \\ ? \end{array} \\ & ?=21+34 \end{aligned} 21+34=$ <br> Calculate the sum of and thirty-four | wenty-one |  |  |


| Concrete | Pictorial | Abstract |
| :---: | :---: | :---: |
| Physically taking away and removing objects from a whole (ten frames, Numicon, cubes and other items such as beanbags could be used). $4-3=1$ | Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used. | $\begin{gathered} 4-3= \\ =4-3 \end{gathered}$4  <br> 3 $?$ |
| Counting back (using number lines or number tracks) children start with 6 and count back 2. $6-2=4$ | Children to represent what they see pictorially e.g. | Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line |
| Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used). <br> Calculate the difference between 8 and 5 . | Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate. | Find the difference between 8 and 5. $8-5$, the difference is ? <br> Children to explore why $9-6=8-5=7-4$ have the same difference. |



| Concrete | Pictorial | Abstract |
| :---: | :---: | :---: |
| Repeated grouping/repeated addition $3 \times 4 / 4+4+4$ <br> There are 3 equal groups, with 4 in each group. | Children to represent the practical resources in a picture and use a bar model. | $\begin{array}{r} 3 \times 4=12 \\ 4+4+4=12 \end{array}$ |
| Number lines to show repeated groups- $3 \times 4$ <br> Cuisenaire rods can be used too. | Represent this pictorially alongside a number line e.g.: | Abstract number line showing three jumps of four. $3 \times 4=12$ |
| Use arrays to illustrate commutativity counters and other objects can also be used. <br> $2 \times 5=5 \times 2$ | Children to represent the arrays pictorially. | Children to be able to use an array to write a range of calculations e.g. $\begin{aligned} & 10=2 \times 5 \\ & 5 \times 2=10 \\ & 2+2+2+2+2=10 \\ & 10=5+5 \end{aligned}$ |



| Concrete | Pictorial | Abstract |
| :---: | :---: | :---: |
| Sharing using a range of objects. $6 \div 2$ | Represent the sharing pictorially. | $6 \div 2=3$3 3 <br> Children should also be encouraged to use their 2 times tables facts. |
| Repeated subtraction using Cuisenaire rods above a ruler. $6 \div 2$ <br> 3 groups of 2 | Children to represent repeated subtraction pictorially. | Abstract number line to represent the equal groups that have been subtracted. |
| Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3=55 \times 3=1515 \div 5=33 \times 5$ $=15$ | Draw an array and use lines to split the array into groups to make multiplication and division sentences. | Find the inverse of multiplication and division sentences by creating four linking number sentences. $\begin{aligned} & 7 \times 4=28 \\ & 4 \times 7=28 \\ & 28 \div 7=4 \\ & 28 \div 4=7 \end{aligned}$ |

## Conceptual variation; different ways to ask children to solve $18 \div 3$

| 6 | 6 | 6 | Mai swam 6 lengths each time she went swimming. <br> She swam 18 lengths one week? How many times did she go swimming that week? |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc$ | $\begin{array}{lllllll}0 & 3 & 6 & 9 & 12 & 15 & 18\end{array}$ <br> What is the calculation? What is the answer? |

